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دینامیک سولیتونی جاذب اشباع‌پذیر حاکم بر نانو ذرات کلوییدی

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چکیده – این مقاله یک حل ساده اما جامع را برای معادله هاوس- که برای توصیف دینامیک قفل زنی مد بکار می‌رود- به منظور مدلسازی جذب اشباع‌پذیر در نانوذرات کلوییدی ارائه می‌کند. تشکیل سولیتون بعنوان ساز و کار اصلی شکل گیری پالس فرض گردیده‌است. مدل گاز غیر ایده-آل برای نانوذرات بکار گرفته شده‌است. فرایند جاذب اشباع‌پذیر به شکل قفل زنی انفعالی شناسایی می‌شود. نتایج حاصل از مدل توافق خوبی با مشاهدات تجربی دارد؛ طی این مشاهدات، نانوذرات کلوییدی محیط‌های مناسبی برای هدف استفاده به عنوان جاذب اشباع‌پذیر معرفی شده‌اند.

کلید واژه- جاذب اشباع‌پذیر، سولیتون، قفل زنی انفعالی، نانوذرات کلوییدی

Soliton Dynamics of Saturable Absorber in Colloidal Nanoparticles

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Abstract- This paper presents a simple, but comprehensive solution of Haus equation – to describe the dynamics of mode-locking- to model Saturable Absorption in colloidal nanoparticles. Soliton formation is considered as the main mechanism of pulse shaping. Non-ideal gas model for nanosusensions nonlinearity is utilized. Saturable Absorber procedure is detected as passive mode-locking. The results show a good matching with the experimental observations in which the nanosuspensions have introduced as suitable media for Saturable Absorption.

Keywords: Saturable Absorption, Soliton, Passive mode-locking, Colloidal nanoparticles

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1 Introduction

Nanoparticles and Colloidal nanosuspensions are well-known for their high nonlinear response even at optically low intensities; their high performance of controlling light with light predicts the promising future of advances in all-optical devices and systems. Recently, Alexander Shamray and his group have experimentally shown that the optical bistabiity in colloidal solution of LaF_3:Er,Yb nanocrystals is truly attainable at low optical power[1]. In spite of multiple studies on nanosuspensions nonlinearity and Saturable Absorption (SA) via nanosuspensions [2-5], there seems to be a lack of theoretical model based on intracavity dominating equations to describe the dynamics of SA through these media.

2 Theoretical description of problem

Theoretical dynamics of pulse-shaping can be described by the Haus equation of mode-locking [6]:

$$T_R \frac{\partial A(T,t)}{\partial T} = -\mathrm{i}D\frac{\partial^2 A}{\partial t^2} + i\gamma|A|^2 A + \left[g - l + D_g \frac{\partial^2}{\partial t^2} - q(T,t)\right]A(T,t) \quad (1)$$

Where, $A(T,t)$ is slowly varying field envelop, T is time scaled to one cavity round trip T_R, t is time scaled to pulse duration, D is Group Velocity Dispersion (GVD) and D_g is gain dispersion; $\gamma = \frac{2\pi}{\lambda_0} n_2$ is the nonlinear coefficient required for Self Phase Modulatiom (SPM) whereas λ_0 is the center wavelength of the pulse, n_2 is the nonlinear refractive index of nanosuspension; g and l are the gain and loss of the cavity respectively; $q(T,t)$ is the response of the absorber. For simplicity, $g-l$ is substituted by the quantity *NET* gain. It should be noted that intracavity loss l is quite different from the loss due to absorption of the nonlinear media; the latter is postponed to be discussed. The corresponding pulse energy can be written as:

$$E = \int_{-T_R/2}^{T_R/2} |A(T,t)|^2 dt \quad (2)$$

2.1 Soliton Regime

Soliton formation is considered as the dominant pulse-shaping mechanism. The function to describe the pulse shape is given below:

$$f(t) = \sqrt{\tfrac{1}{2\tau}}\,\mathrm{sech}(\tfrac{t}{\tau}) \quad (3)$$

τ is pulse width which is defined as the full-width at half-maximum (FWHM) of the soliton. Soliton formation is a consequence of the balance between GVD and SPM inside the cavity; this in turn leads to the equation $\frac{|D|}{\tau^2} = \frac{\gamma E}{4\tau}$. The equation can be written as the pulse width related to the energy of the pulse:

$$\tau = \frac{4|D|}{\gamma E} \quad (4)$$

On the other hand, energy rate equation is proved to be written as[6]:

$$T_R \frac{\partial E}{\partial T} = 2g_{NET} - 2q(E) \quad (5)$$

Where:

$$g_{NET} = \frac{g_{0,NET}}{1 + \frac{E}{E_s}} \quad (6)$$

Through the steady state, the ratio between intracavity GVD and gain dispersion is set to be at a certain value[6].

It is inevitable to introduce TPA (Two Photon Absorption) loss through the calculations in order to measure Minimum Pulse Energy (MPE) needed for the desired case of single pulse mode locking. Equation describing MPE is obtained according to [6]:

$$E_{\min,SSA} = \sqrt[3]{\frac{q_M E_S}{\alpha_{TPA}}} \quad (7)$$

Here, q_M is the maximum absorber response, $\alpha_{TPA} \propto \frac{\alpha\gamma}{12D}$ is the loss pertained to TPA. The quantity α is the aforementioned absorption of nonlinear medium due to Rayleigh scattering.

2.2 Non-ideal gas nonlinearity model of nanosuspensions

According to this approach, the first order nonlinear refractive indices of n_2 is yielded as:

$$n_2 = \left(\frac{n_{2k}}{1 + 2(B_2/V_p)f_0 + 3(B_3/V_p^2)f_0^2}\right) \quad (8)$$

In these equations, n_{2k} is artificial Kerr nonlinearity, B_2 and B_3 are second and third

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Virial coefficients, V_p is the volume of nanoparticle, f_0 is the field free background filling factor of the colloidal nanoparticles.
The first nonlinear loss of TPA due to Rayleigh scattering is given by $\alpha = \frac{1}{2}\frac{\sigma\rho_0}{I_c(1+2(B_2/V_p)f_0+3(B_3/V_p^2)f_0^2)}$ where ρ_0 is the initial nanoparticle density inside the colloid, I_c pertains to the light intensity keeping the limit of exponential model for nonlinearity and $\sigma = \frac{128\pi^5 a^2 n_b^4}{3}\left(\frac{a}{\lambda_0}\right)^4\left(\frac{m^2-1}{m^2+2}\right)^2$ is scattering cross section; n_b is background refractive index of colloid and $m = n_p / n_b$ is the ratio of nanoparticles refractive index to n_b.

3 Analytical Results and Discussion

For a sinusoidal response of the absorber[8], one pulse operation is assumed. Equation (9) performs a simple but comprehensive analytical solution of the equation (5) to describe the dynamics of soliton regime inside mode-locked cavity for successive cavity round trips.Once the energy inside the cavity is increased, SA response will be strengthened and the intracavity energy will be diminished to its primary value. This implies that the field envelop inside the cavity is passively mode-locked.

$$E(T) = \frac{1}{2}\frac{g_{0,NET}}{1+\frac{E(T-T_R)}{E_s}}\times \alpha_{TPA}(1-q_M\cos(\pi E(T-T_R)))E(T-T_R) \quad (9)$$

The iterative form of equation (9) explicates the state of the system as a function of q_M and E_s. For sufficiently small values of q_M and E_s, cw stable operation will be provided if the gain of the medium is adequate. To ensure that high efficient laser cavity is attainable, q_M should be increased; afterward, above a certain threshold value of E_s, the system transforms to mode-locking state. Figure 1 shows system transition from the primary cw state toward the chaotic state as q_M and E_s are increased.

3.1 Effect of Nanoparticle characteristics on the system state

Experimental measured data are taken from Majles Ara, *et al.*[3]. Calculations based on the presented model show that for the nanoparticles density order of 10 times larger than what is assumed, steady state mode-locking will be vanished and the system will experience a fully chaotic regime. Conversely, for 10 times lower order steady state mode-locking regime will no more be available.

3.2 MPE required for passively mode-locking

Equation (7) stands for MPE required for steady state mod-locking. Figure 2.a shows the dependence of MPE on the average diameter of nanoparticles. It can be seen that there is an optimum point in which the MPE is increased over/under the value. The procedure offers to use small sizes of nano-scaled particles. Indebted to the large values of α and γ pertained to nanosuspensions, researchers believe/experience that passive mode-locking is attainable at extremely low powers [4-5]. Infinitesimal experimental reported values of D inside nanosuspensions intensify this opinion (refer to equation (8)).

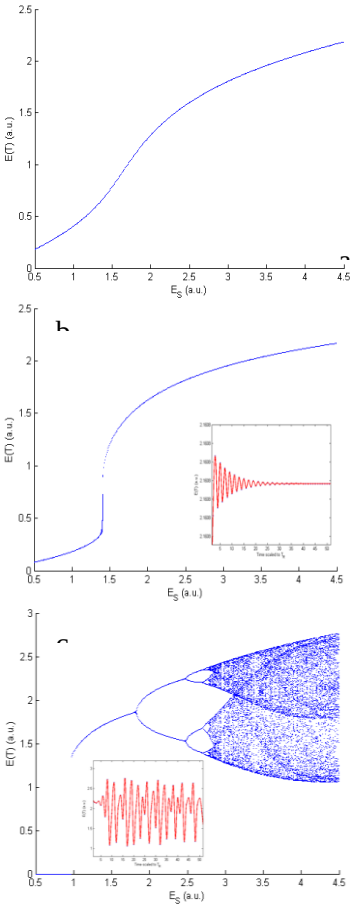


Figure 1: All available states of the system inside the cavity as a function of E_s, a) cw steady state, $q_M = 0.2$, b) Bistable state (Inset shows how the system

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transforms to upper stable state), $q_M = 0.3$, c) Chaotic state (Inset shows how the system has instability over time), $q_M = 0.6$.

4 Conclusion

A simple, but comprehensive solution of Haus equation is presented. Using the Non-ideal gas model of nonlinearity for colloidal nanoparticles, a model is constructed to investigate Saturable Absorption inside nanosuspensions. These results seem to be truly matched with experimental observations.

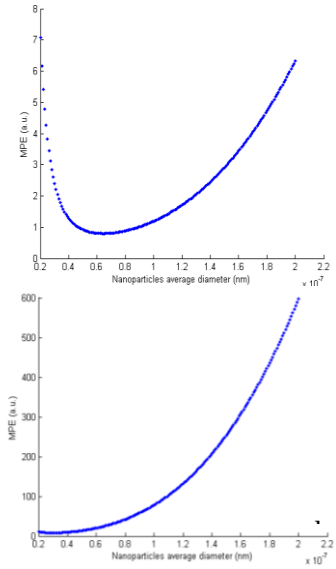


Figure 2: MPE vs. nanoparticles size a)for assumed nanoparticles density b) for 10 times higher nanoparticles density

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